## Solving Related Rates Problems:

- Find an equation that ties your variables together.
- You may now plug in any constant value. Do not plug in any value that changes.
- Differentiate your equation with respect to time.
- Plug in all variables. If you have more than one unknown, you will most likely use your original equation to find the missing value.
- Label your answers in terms of the correct units and be sure that you answered the question asked!

1. A spherical bubble is being blown up. The volume is increasing at the rate of $9 \mathrm{~mm}^{3}$ per second. At what rate is the radius increasing when the radius is 3 mm ?
2. A cylindrical tumbler with a radius of 3 cm has its height increasing at a rate of $2.5 \mathrm{~cm} / \mathrm{sec}$. Find the rate of change of the volume of the cylinder when the height is 12.56 cm .
3. Tracking a rocket: A spy tracks a rocket through a telescope to determine its velocity. The rocket is traveling vertically from a launching pad located 10 km away, as in the figure. At a certain moment, the spy's instruments show that the angle between the telescope and the ground is equal to $\frac{\pi}{3}$ and is changing at a rate of $0.5 \mathrm{rad} / \mathrm{min}$. What is the rocket's velocity at that moment?

4. A spherical hot air balloon is being inflated. If air is blown into the balloon at the rate of $2 \mathrm{ft}^{3} / \mathrm{sec}$,
a. Find how fast the radius of the balloon is changing when the radius is 3 ft .
b. Find how fast the surface area is increasing at the same time.
5. You are looking at the New York ball drop on New Year's Eve at a distance of 100 m away from the base of the structure. If the ball drops at a constant rate of $2 \mathrm{~m} / \mathrm{s}$, what is the rate of change of the angle between you and the ball when the angle is $\frac{\pi}{4}$ ?
