

Warm Up

Turn and Talk...

1. What do you think recursion means?
2. What is a sequence?
3. What is a term?
4. What is an Arithmetic Sequence?
5. What is a Geometric Sequence?

Unit 1

Sequences and Series

Recursion

Each step of a pattern is dependent on the previous step

Sequence

An ordered list of numbers
(example: 2, 4, 6, ...)

Term

Each member of a sequence is
called a term

Notation:

$$u_1 = 2 \text{ (1st term)}$$

$$u_3 = 6 \text{ (2nd term)}$$

$$u_n = n^{\text{th}} \text{ term}$$

Arithmetic Sequence

An adding sequence -- we find the next term by adding (or subtracting) to the previous term.

Notation: u_1 = first term

Geometric Sequence

A multiplication sequence -- we find the next term by multiplying (or dividing) the previous term.

Notation: u_0 = first term

Arithmetic sequences



We talk about the *common difference* or what the pattern is changing by

$$u_3 - u_2 = d \text{ (common difference)}$$

$$u_{10} - u_9 = d$$

Geometric sequences

We talk about the *common ratio* or what the pattern is changing by

$$u_3/u_2 = r \text{ (common ratio)}$$

$$u_{10}/u_9 = r$$

Recursive Rules

In an arithmetic sequence we can find the next term by:

$$u_n = u_{(n-1)} + d$$

Handwritten annotations:

- what I want* (with an arrow pointing to u_n)
- previous term* (with an arrow pointing to $u_{(n-1)}$)
- common diff* (with an arrow pointing to $+d$)

In a geometric sequence the subsequent term is found by:

$$u_n = u_{(n-1)} * r$$

Summary

Geometric Sequence

First term is U_0

Multiplying (or dividing)

Common ratio (r) .

Next term: $U_n = U_{(n-1)} * r$.

Arithmetic Sequence

First term is U_1

Adding (or subtracting)

Common difference (d) .

Next term: $U_n = U_{(n-1)} + d$.

1) Write the first 4 terms of each sequence.

a) $u_1 = 20$

$u_n = u_{(n-1)} + 6$ ~~where $n > 2$~~

b) $u_1 = 47$

$u_n = u_{(n-1)} - 3$ ~~where $n > 2$~~

c) $u_0 = 32$

$u_n = 1.5 * u_{(n-1)}$ ~~where $n > 1$~~

d) $u_1 = -18$

$u_n = u_{(n-1)} + 4.3$ ~~where $n > 2$~~

$$U_n = U_{(n-1)} + 6$$

$$U_6 = U_5 + 6 = 44 + 6 = 50$$

20, 26, 32, 38, 44, ...

↑
1st

↑
2nd

↑
3rd

↑
4th

↑
5th

$n = 1$

2

3

4

5